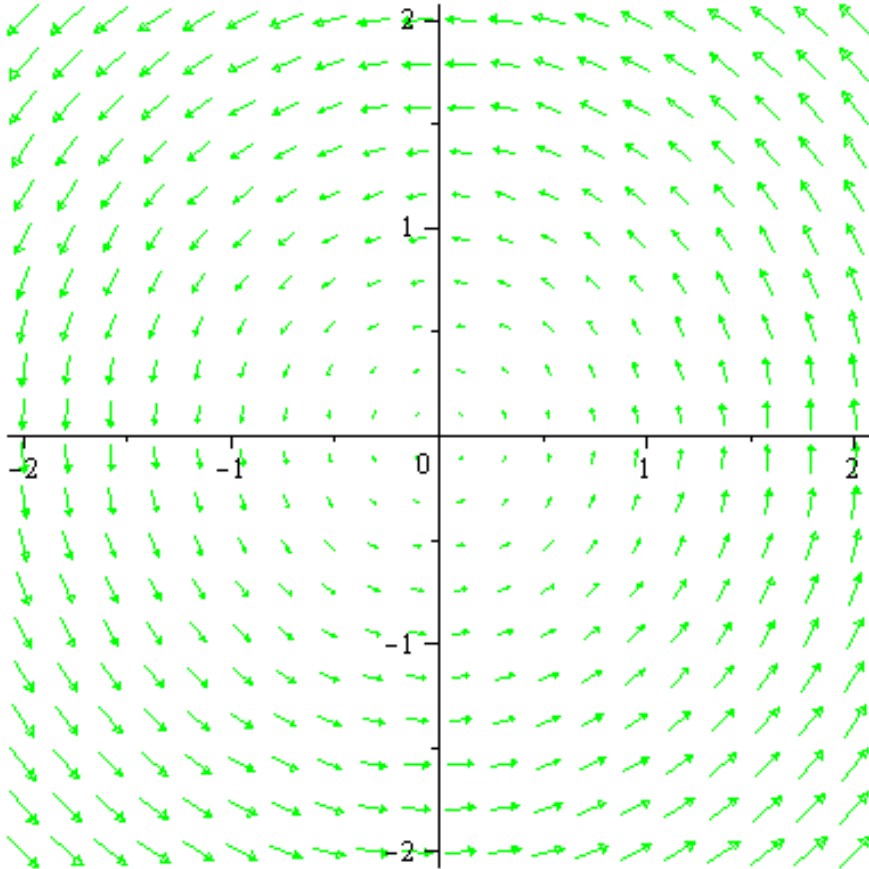




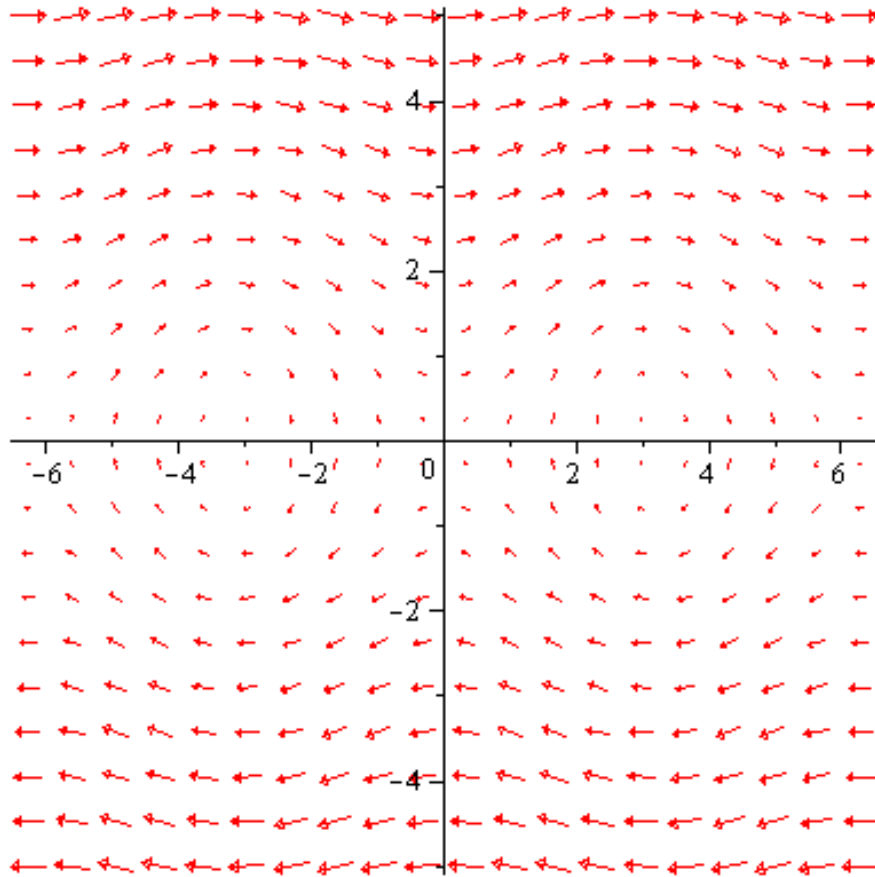
Medan Vektor

$$f(x, y) = -y \hat{i} + x \hat{j}$$



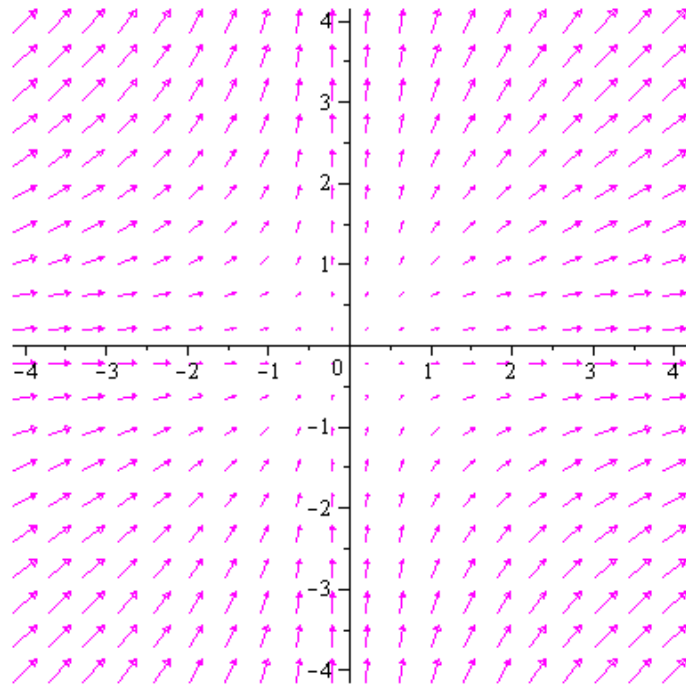


$$f(x, y) = y \hat{i} + \sin(x) \hat{j}$$



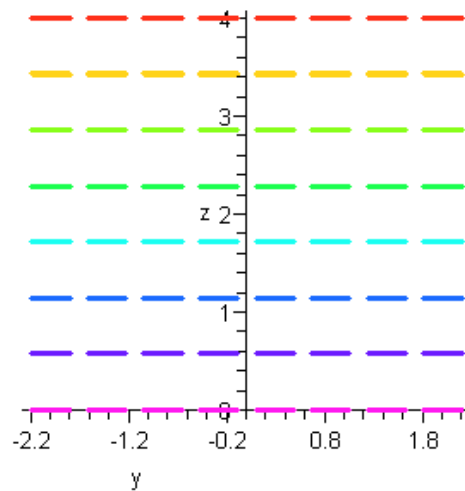
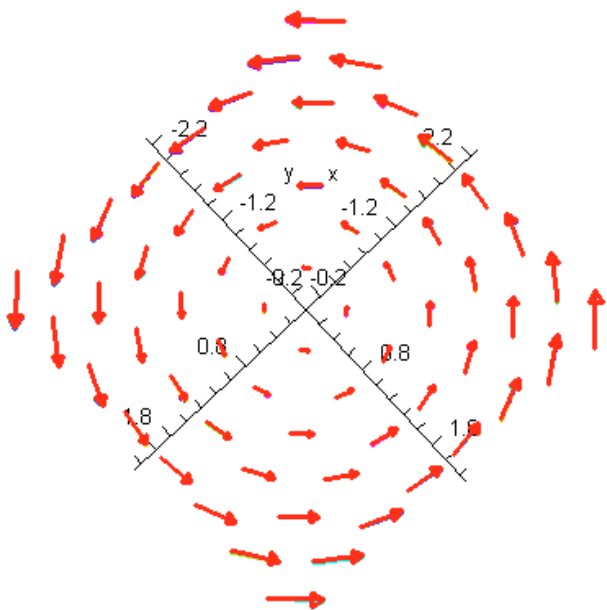


$$f(x, y) = \ln(1 + x^2) \hat{i} + \ln(1 + y^2) \hat{j}$$

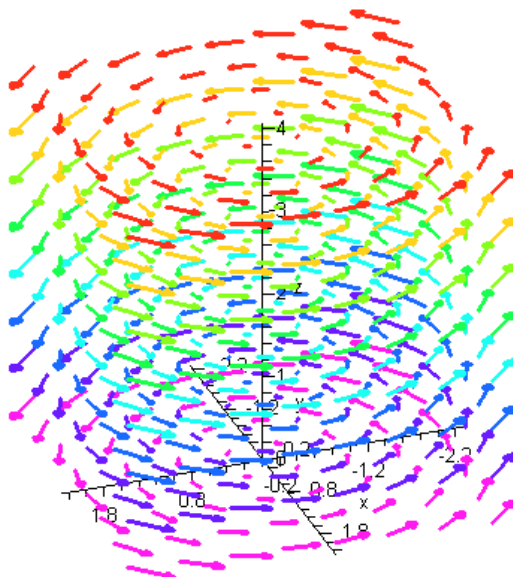


$$\text{HURICANE : } f(x, y, z) = -y \hat{i} + x \hat{j} + 0 \hat{k}$$

Bidang XOY Bidang YOZ

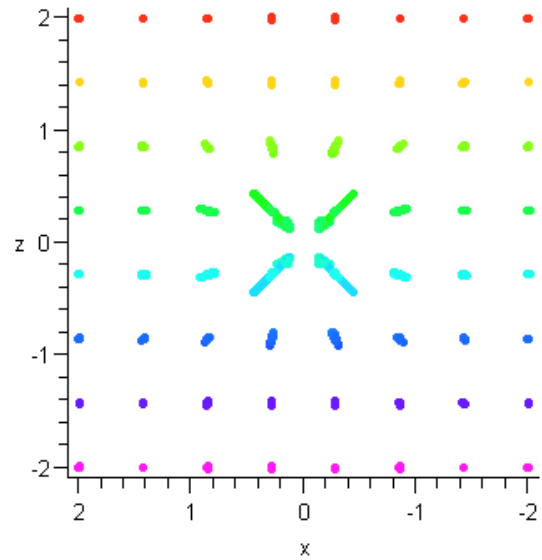
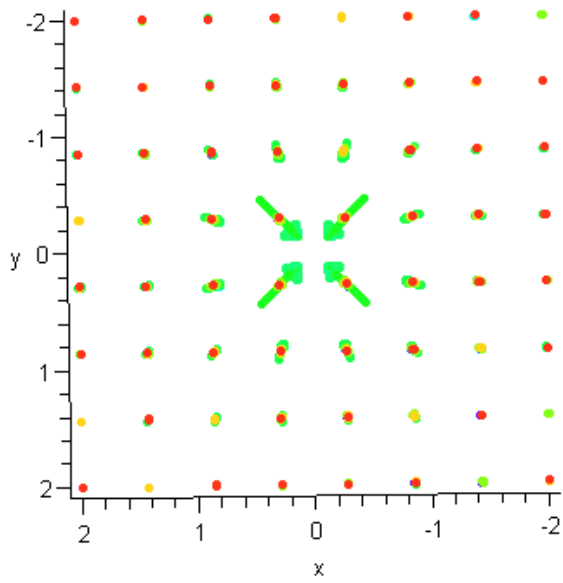


Tiga Dimensi



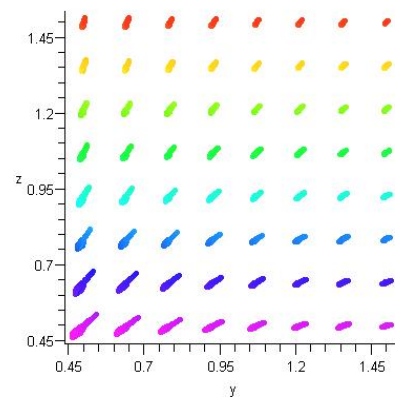
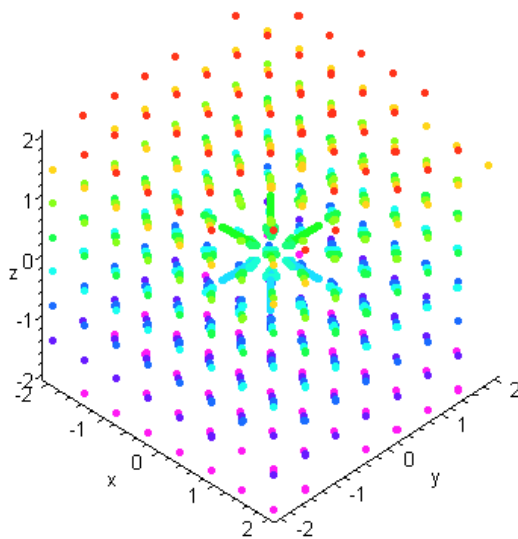


Gravity: $f(x, y, z) = x \hat{i} + y \hat{j} + z \hat{k}$
Bidang XOY Bidang XOZ



Tiga Dimensi

Pada kuadran pertama bidang YOZ





MEDAN GRADIEN

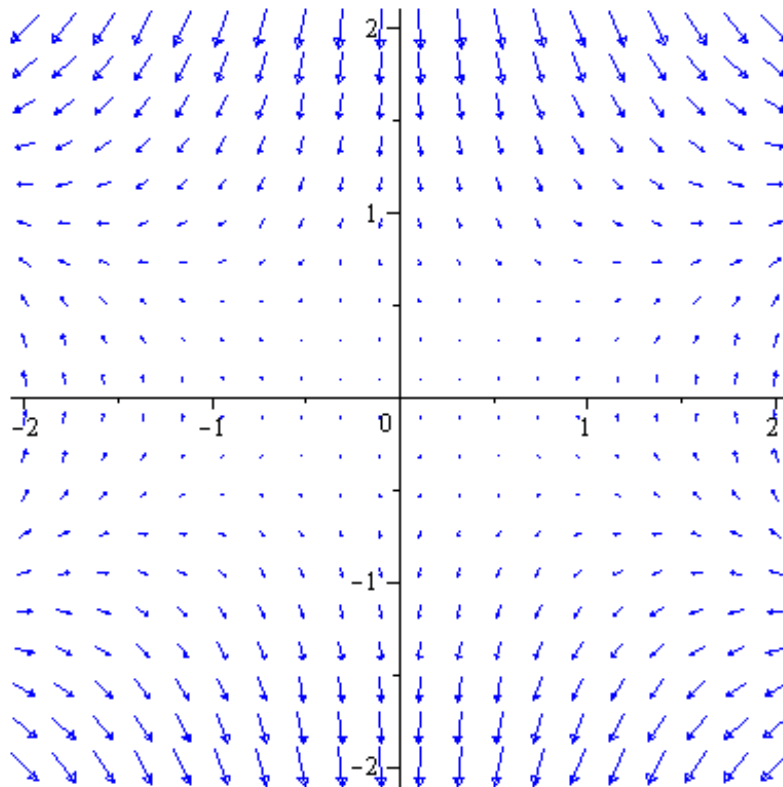
$$f(x, y) = x^2y - y^3$$

Untuk x dan y bertanda sama: arah thd x selalu ke kanan

Untuk x dan y berbeda tanda: arah thd x selalu ke kiri

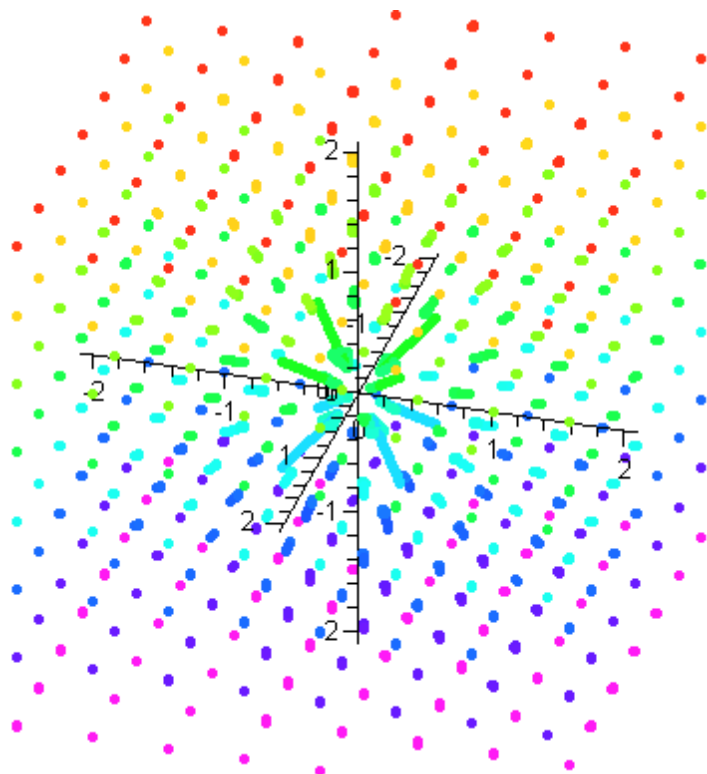
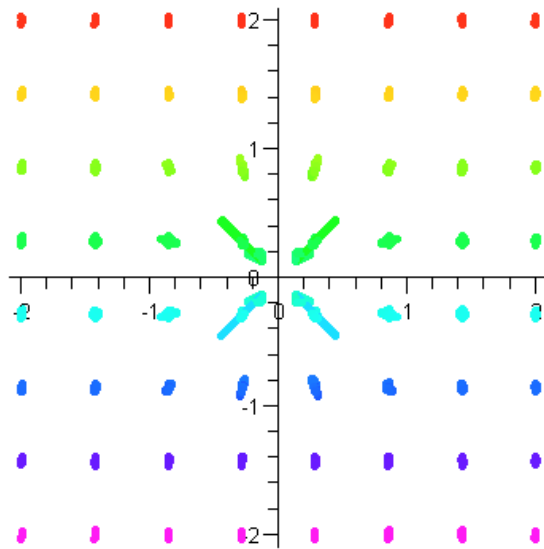
Apabila turunan parsial thd y > 0 maka arah ke atas

Apabila turunan parsial thd y < 0 maka arah ke bawah



$$f(x, y, z) = \frac{1}{\sqrt{x^2 + y^2 + z^2}}$$

Bidang XOZ





Latihan:

1. Tuliskan persamaan parameter untuk garis lurus melalui titik $(2,0,4)$ dan $(-3,0,9)$.
2. Diberikan curva $r(t)$ dan titik P:
$$\mathbf{r}(t) = [3 \cos t, 3 \sin t, 4t], \quad P: (3, 0, 8\pi)$$

Carilah vektor singgung $r'(t)$ di titik P, sketsa gambarnya di bidang XOY dan dimensi 3.
3. Tentukan kurva isoterm (kurva yang memiliki suhu konstan T) dari fungsi berikut: a. $T = xy$ b. $T = \frac{y}{x^2+y^2}$
4. Gambarkan medan vektor dari
$$\mathbf{v} = (x - y)\mathbf{i} + (x + y)\mathbf{j}$$
5. Diberikan $f = x^2 + y^2 - z$, $P: (1, 1, -2)$, $\mathbf{a} = [1, 1, 2]$. Tentukan turunan berarah f terhadap vektor a di titik P.